## Association of Accounting Technicians of Sri Lanka

## Level I Examination - January 2021

## Suggested Answers

(102) BUSINESS MATHEMATICS AND STATISTICS (BMS)

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THE ASSOCIATION OF ACCOUNTING TECHNICIANS OF SRI LANKA Level I Examination - January 2021
(102) BUSINESS MATHEMATICS AND STATISTICS SUGGESTED ANSWERS
(Total 40 Marks)
SECTION - A

## Suggested Answers to Question One:

1.1 Government deduction $=100-45 \%=55 \%$

Last 3 months bill $=$ Rs. 18,000
Deducted amount $=18,000 \times \frac{55}{100}$
Answer (2) - Rs.9,900/- $=$ Rs.9,900
1.2
$P=\frac{P 1}{P 0} \times 100$
$P=\frac{140}{80} \times 100=\underline{\underline{175 \%}} R\|\mid A\| \| A$
Answer (4) - 175\%
1.3

$$
\begin{aligned}
& r=\frac{\left[\mathrm{n} \sum \mathrm{xy}-\sum \mathrm{x} \cdot \sum \mathrm{y}\right]}{\sqrt{\left\{\left[\mathrm{n} \sum \mathrm{x}^{2}-\left(\sum \mathrm{x}\right)^{2}\right] \times\left[\mathrm{n} \sum \mathrm{y}^{2}-\left(\sum \mathrm{y}\right)^{2}\right]\right\}}} \\
& r=\frac{10 \times 130.64-25 \mathrm{X} 50}{\sqrt{\left(10 \times 65.68-25^{2}\right)\left(10 \times 260.48-50^{2}\right)}} \\
& =\underline{\mathbf{+ 0 . 9 7 7}}
\end{aligned}
$$

Answer (1) - +0. 977
(03 marks)
1.4 The mode is the most commonly occurring value in a distribution.

Mode $=17$
Answer (4)-17
(03 marks)
1.5 $S=x r n \quad S=$ interest, $x=75,000, r=12, n=2$

Interest $=75,000 \times 0.12 \times 2$
Interest = Rs.18,000
Answer (3)-Rs.18,000/-
$1.6 x=6,000, \quad n=5, \quad r=0.05$
$P V=\frac{X\left(1-(1+r)^{-n}\right)}{r}$
$P V=\frac{6,000\left(1-1.05^{-5}\right)}{0.05}$
$P V=R s .25,977 \underline{\underline{\mathbf{2 5}, 980}}$
Answer (4) - Rs.25,980/-
(03 marks)
1.7 $\quad P(A \cup B)=P(A)+P(B)-P(A \cap B)$
$P(A \cup B)=0.38+0.22-0.06$
$P(A \cup B)=0.54$
Answer (3) - 0.54
(03 marks)
$\left.1.8 S=X(1+r / N)^{n \times N} S \mathrm{R}_{\mathrm{x}=75,000} \mathrm{~A} \mathrm{n}=2\right\} \mathrm{r} \neq 0.12, \quad N=4$
$S=75,000 \times(1+0.12 / 4)^{2 \times 4}$
$S=95,007.76$
$S=\underline{\text { Rs. } 95,008}$
Answer (1) - Rs.95,008/-
(03 marks)
1.9

| Seasons <br> (quarter) | Seasonal <br> Index(S) | Trend <br> $\mathbf{( T )}$ | Forecasted Sales (T×S) |
| :---: | :---: | :---: | :---: |
| 1st | 0.93 | 7,617 | 7,084 |
| (03marks) $_{\text {2nd }}$ | 0.84 | 7,764 | 6,522 |
| 3rd | 1.09 | 7,912 | 8,624 |
| 4th | 1.14 | 8,060 | 9,188 |

Answer (1) - 7,084, 6,522, 8,624, 9,188
(03 marks)
1.10 $P V=400,000, n=5, r=0.12$

$$
\begin{aligned}
& P V=\frac{X\left(1-(1+r)^{-n}\right)}{r} \\
& 400,000=\frac{X\left(1-1.12^{-5}\right)}{0.12} \\
& X=400,000 \times \frac{0.12}{\left(1-1.12^{-5}\right)} \\
& \underline{X=\text { Rs. } 110,964}
\end{aligned}
$$

Answer (3) = Rs. 110,964
1.11
$\mathrm{A} \longrightarrow$
$\mathrm{B} \longrightarrow$
$\mathrm{C} \longrightarrow$
C
$\mathrm{C} \longrightarrow$
1
2
1.12 $S k=\frac{3(\bar{X}-M d)}{S}$
$S k=$ coefficient of skewness
$\bar{X}=$ mean
$\mathrm{Md}=$ median
$S k=\frac{3(710-690)}{\sqrt{144}} \mathrm{~A} \|$ S = standard deviation
$=\frac{60}{12}$
$=\underline{\underline{5}}$
(02 marks)
$1.13 a=4, d=3, n=10$
$T_{n}=a+(n-1) d$

$$
=4+(10-1) \times 3
$$

$$
=4+9 \times 3
$$

$$
=\underline{\underline{31}}
$$

1.14 Statement is "True"
(01 mark)
1.15 Statement is "False"
(01 mark)
(Total 40 marks)

Suggested Answers to Question Two:

## Chapter 1 - Fundamental Concepts of Mathematics

(a)

$$
\begin{array}{cl}
3(4 x+2) & =30 \\
12 x+6 & =30 \\
12 x & =24 \\
\boldsymbol{x} & =\mathbf{2} \\
\hline \hline
\end{array}
$$

(b)

$$
\begin{align*}
& 3 x+5 y=-7-(1) \\
& 11 x-8 y=27 \tag{2}
\end{align*}
$$

(1) $\mathrm{x} 8 \rightarrow 24 x+40 \mathrm{y}=-56$ - (3)
(2) $\mathrm{x} 5 \rightarrow 55 \mathrm{x}-40 \mathrm{y}=135$ - (4)
(3) x (4) $\rightarrow 79 x=79$

$$
x=1
$$

Applying $x=1$ to (1)
$3 x+5 y=-7$
$3 \times 1+5 y=-7$
$5 y=-7-3$
$y \quad=\frac{-10}{5}$

$$
\begin{gathered}
y=-2 \\
\underline{x}=1 \quad y=-2
\end{gathered}
$$

(c)

$$
\begin{aligned}
x & =800, \mathrm{r}=5 \%, \mathrm{n}=4, \mathrm{~S}=? \\
S & =x(1+r)^{n} \\
S & =800(1+0.05)^{3} \\
& =800 \times 1.05^{3} \\
& =\text { Rs. } 926.10
\end{aligned}
$$

## Suggested Answers to Question Three:

## Chapter 3-Financial Operative Measures for Business

(a) (i)
TC $=V C+F C$
TC = Total cost
TC $=2 q^{2}-12 q+12,000$
$\mathrm{VC}=$ Variable cost
FC = Fixed cost

Total Revenue Function (TR) = Demand Function $\times$ Number of Units
$T R=D \times q$
$T R=(q+8) \times q$
$\underline{\underline{T} R=q^{2}+8 q}$
(04 marks)
(ii) Profit Function $=T R-T C$

$$
\begin{aligned}
&=q^{2}+8 q-\left(2 q^{2}-12 q-12 q+12,000\right) \\
&=q^{2}+8 q-2 q^{2}+12 q-12,000 \\
&=-q^{2}+20 q-12,000 \\
& \frac{d p}{d x}=-2 q+20=0 \\
& 2 q=20 \\
& \underline{q}=10 \\
& \frac{D^{2} p}{D X^{2}}=-2<0 \\
& \underline{q}=10 \\
& \text { Answer: }
\end{aligned}
$$

Alternative Answer:

$$
\begin{aligned}
& T R=q^{2}+8 q \\
& M R=2 q+8 \\
& T C \quad=12,000+2 q^{2}-12 q
\end{aligned}
$$

$$
M C=4 q-12
$$

Profit is maximum, When MR = MC

$$
\begin{aligned}
2 q+8 & =4 q-12 \\
X & =10
\end{aligned}
$$

Number of units are 10
(b)
$T R=2 q^{2}+4 q \quad T C=2 q^{2}+2 q+200,000$
At the Break Even Point;

$$
\begin{aligned}
T R & =T C \\
2 q^{2}+4 q & =2 q^{2}+2 q+200,000 \\
2 q^{2}-2 q^{2}+4 q-2 q & =200,000 \\
2 q & =200,000 \\
q & =100,000
\end{aligned}
$$

Break-Even Quantity $=\mathbf{1 0 0 , 0 0 0}$ units

## Suggested Answers to Question Four:

## Chapter 5 - Comparing Two Quantitative Variables

(a) $\sum \mathrm{X}=420, \sum \mathrm{Y}=360, \sum \mathrm{XY}=27,354, \quad \sum \mathrm{X}^{2}=33,408, \mathrm{n}=6$

| $\boldsymbol{x}$ | $\boldsymbol{y}$ | $\boldsymbol{x}^{\mathbf{2}}$ | $\boldsymbol{x y}$ |
| :---: | :---: | ---: | ---: |
| 38 | 42 | 1,444 | 1,596 |
| 42 | 44 | 1,764 | 1,848 |
| 60 | 52 | 3,600 | 3,120 |
| 80 | 71 | 6,400 | 5,680 |
| 90 | 75 | 8,100 | 6,750 |
| 110 | 76 | 12,100 | 8,360 |
| $\mathbf{4 2 0}$ | $\mathbf{3 6 0}$ | $\mathbf{3 3 , 4 0 8}$ | $\mathbf{2 7 , 3 5 4}$ |

$\mathrm{b}=\frac{\mathrm{n} \sum \mathrm{XY}-\sum \mathrm{X} \cdot \sum \mathrm{Y}}{\left(\mathrm{n} \sum \mathrm{X}^{2}-\left(\sum \mathrm{X}\right)^{2}\right)}$
$\mathrm{b}=\frac{(6 \times 27,354)-(420 \times 360)}{(6 \times 33,408)-\left(420^{2}\right)}$
b $=\frac{164,124-151,200}{200,448-176,400}$
$b=\frac{12,924}{24,048}$
$b=0.54$
$a=\bar{Y}-b \bar{X}$
$a=\frac{360}{6}-\left[0.5374 \times \frac{420}{6}\right]$
$a=60-37.56$
$a=22.38$
Therefore least square regression line is,
$Y=a+b x$
$\underline{Y}=22.38+0.54 x$
(07 marks)
(b) Healthcare expense is Rs.75,000/-

Then substitute $\mathrm{x}=75$

$$
\begin{aligned}
& Y=22.38+0.54 x \\
& Y=22.38+0.54 \times 75 \\
& Y=62.88
\end{aligned}
$$

Average life expectancy $=\underline{\mathbf{6 3} \text { years }}$

## Suggested Answers to Question Five:

## Chapter 4 - Data Presentation and Descriptive Measures

(a) Median
$n=40$
$\frac{n}{2}=20$,
$\mathrm{L}_{1}=19.5, \mathrm{Fc}=5, \mathrm{fm}=15$,
Median Class = 29.5-19.5
$\equiv 10$
$\operatorname{Md}=\mathrm{L}+\frac{\left(\frac{n}{2}-F c\right)}{f m} \times c$
$\operatorname{Md}=19.5+\frac{(20-5)}{15} \times 10$
$M d=29.5$

Median of the monthly salary = Rs.29,500
(b) Mean

| Monthly Salary <br> (Rs.'000) | Mid Point <br> $\boldsymbol{x}$ | No. of <br> Employees | $\boldsymbol{f} \boldsymbol{x}$ | $\boldsymbol{f} \boldsymbol{x}^{\mathbf{2}}$ |
| :---: | :---: | :---: | :---: | ---: |
| $10-19$ | 14.5 | 5 | 72.5 | $1,051.25$ |
| $20-29$ | 24.5 | 15 | 367.5 | $9,003.75$ |
| $30-39$ | 34.5 | 8 | 276 | 9,522 |
| $40-49$ | 44.5 | 4 | 178 | 7,921 |
| $50-59$ | 54.5 | 5 | 272.5 | $14,851.25$ |
| $60-69$ | 64.5 | 3 | 193.5 | $12,480.75$ |

Mean $=\frac{\sum f x}{\sum f}=\frac{1360}{40}=\underline{\underline{34}}$
(03 marks)
(c) Standard Deviation $=\sqrt{\frac{\sum f x^{2}}{\sum f}-\left[\frac{\sum f x}{\Sigma f}\right]^{2}}$

OR

$$
\begin{aligned}
\text { Standard Deviation } & =\sqrt{\frac{54,830}{40}-\left[\frac{1,360}{40}\right]^{2}} \\
& =\sqrt{1,370.75-34^{2}} \\
& =\sqrt{1,370.75-1,156} \\
& =\sqrt{214.75} \\
& =1 \mathbf{1 4 . 6 5}
\end{aligned}
$$

$$
\begin{aligned}
& =\sqrt{\frac{\sum f x^{2}-x}{\sum f}-x} \\
& =\sqrt{\frac{54,830}{40}-34^{2}} \\
& =\sqrt{1,370.75-1,156} \\
& =\sqrt{214.75} \\
& \equiv 14.65
\end{aligned}
$$

Suggested Answers to Question Six:
(A)

## Chapter 2 - Financial Mathematics for Business

(a)

| Year | Project A | Project B | DF @10\% | Project A <br> PV | Project B <br> PV |
| :---: | ---: | ---: | ---: | ---: | ---: |
| $\mathbf{0}$ | $(160,000)$ | $(130,000)$ | 1 | $(160,000)$ | $(130,000)$ |
| $\mathbf{1}$ | 20,000 | 45,000 | 0.909 | 18,180 | 40,905 |
| $\mathbf{2}$ | 50,000 | 65,000 | 0.826 | 41,300 | 53,690 |
| $\mathbf{3}$ | 90,000 | 50,000 | 0.751 | 67,590 | 37,550 |
|  |  |  |  | $\mathbf{( 3 2 , 9 3 0 )}$ | $\mathbf{2 , 1 4 5}$ |

$$
\begin{aligned}
\mathrm{NPV}_{B} & =\text { PV-I } \\
& =-130,000+132,145 \\
\underline{N P V} & =+2,145
\end{aligned}
$$

(b) NPV is positive for project B. Project A has a negative NPV.

Therefore, company should invest in project $B$.
(B)

## Chapter 6 - Probability and its Applications

| $\boldsymbol{X}$ | $\boldsymbol{P}(\boldsymbol{X})$ | $\boldsymbol{X P}(\boldsymbol{x})$ |
| :---: | :---: | :---: |
| 2 | 0.14 | 0.28 |
| 3 | 0.13 | 0.39 |
| 4 | 0.23 | 0.92 |
| 5 | 0.24 | 1.20 |
| 6 | 0.26 | 1.56 |
|  | $\mathbf{1 . 0 0}$ | 4.35 |

$$
E[X]=\sum X \times P(x)=\underline{\mathbf{4 . 3 5}}
$$

$$
\begin{aligned}
& \mathrm{NPV}_{\mathrm{A}}=\mathrm{PV}-\mathrm{I} \\
& =-160,000+127,070 \\
& \underline{N P V=-32,930} \\
& \text { So, NPV of Project } A=-32,930 \\
& \text { NPV of Project B }=\underline{\underline{+2,145}} \\
& \text { OR } \\
& \text { Project A } \\
& N P V=\frac{20,000}{1.1^{1}}+\frac{50,000}{1.1^{2}}+\frac{90,000}{1.1^{3}}-160,000 \\
& \begin{aligned}
N P V= & =127,122.46-160,000 \_A \| A \\
& \underline{\underline{=-32,877.54}}
\end{aligned} \\
& \text { Project B } \\
& N P V=\frac{45,000}{1.1^{1}}+\frac{65,000}{1.1^{2}}+\frac{50,000}{1.1^{3}}-130,000 \\
& N P V=132,193.84-130,000 \\
& \text { = 2,193.84 }
\end{aligned}
$$

## (C)

## Chapter 6 - Probability and its Applications

(a)

$\varepsilon$ - All the people in a survey
C - People who are having a computer
$S$-People who are having smart phone
(b)

$$
P\left(\frac{S}{C}\right)=\frac{P(S \cap C)}{P C}=\frac{\mathbf{1 7}}{\mathbf{5 4}}
$$

(D)

Chapter 6-Probability and its Applications
X : time taken to service a car (hours)
$\mu=1.35 \quad \sigma=0.35$
$z=\frac{(X-\mu)}{\sigma}$
$z=\frac{x-1.35}{0.35}$

$Z=\frac{1-1.35}{0.35}$
$Z=-1.0$
Probability $\quad=(X<1.0)$
$=0.5-0.3413$
$=0.1587$ or $\mathbf{1 5 . 8 7 \%}$
The probability that the car servicing center takes less than one hour to service a car is 0.1587 or 15.87\%.

## Notice:

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